

## Factorising - 3 terms where coefficient of $x^2 \neq 1$ ( $a \neq 1$ )

$ax^2 + bx + c$  \*always check if a common factor can be removed first (to make  $a = 1$ ), if not follow this method \*

- ① find a factor pair of ' $a \times c$ ' that adds to ' $b$ '
- ② replace ' $bx$ ' by  $x \times$  each factor.
- ③ Separate four terms and factorise as  $2 \times 2$  terms
- ④ check that brackets are equal
- ⑤ factorise again to finish with 2 brackets.

eg  $2x^2 + 5x + 3$       ①  $axc = 2 \times 3 = 6$      $\begin{matrix} 1 & -1 \\ 6 & -6 \end{matrix} \begin{pmatrix} 2 \\ 3 \end{pmatrix} \begin{matrix} -2 \\ -3 \end{matrix} \}$  adds to 5?

$$= \underbrace{2x^2 + 2x} + \underbrace{3x + 3}$$

Always ensure that number order of  $x$ s allow for factorising

$$\begin{aligned} \text{③} &= 2x(x+1) + 3(x+1) \\ &= (x+1)(2x+3) \end{aligned}$$

- ④  $\checkmark$  brackets are the same ( $x+1$ )  
⑤ take ( $x+1$ ) out as common factor and put what's left in second bracket.

eg  $3x^2 + 2x - 5$       ①  $axc = -15$      $\begin{matrix} 1 & -1 \\ -15 & 15 \end{matrix} \begin{pmatrix} -3 \\ 5 \end{pmatrix} \begin{matrix} 2 \\ 3 \end{matrix} \}$  adds to 2?

$$\begin{aligned} &= \underbrace{3x^2 - 3x} + \underbrace{5x - 5} \\ &= 3x(x-1) + 5(x-1) \\ &= (x-1)(3x+5) \end{aligned}$$

eg  $4x^2 + 11x - 3$       ①  $axc = -12$      $\begin{matrix} 1 & -1 \\ -12 & 12 \end{matrix} \begin{pmatrix} -1 \\ 3 \end{pmatrix} \begin{matrix} 2 & -2 \\ -6 & 6 \end{matrix} \begin{matrix} -3 & -3 \\ 4 & 4 \end{matrix} \}$  adds to 11?

$$\begin{aligned} &= \underbrace{4x^2 + 12x} - \underbrace{x - 3} \\ &= 4x(x+3) - 1(x+3) \\ &= (x+3)(4x-1) \end{aligned}$$

Remember you can always check by expanding again to see if you get original expression!